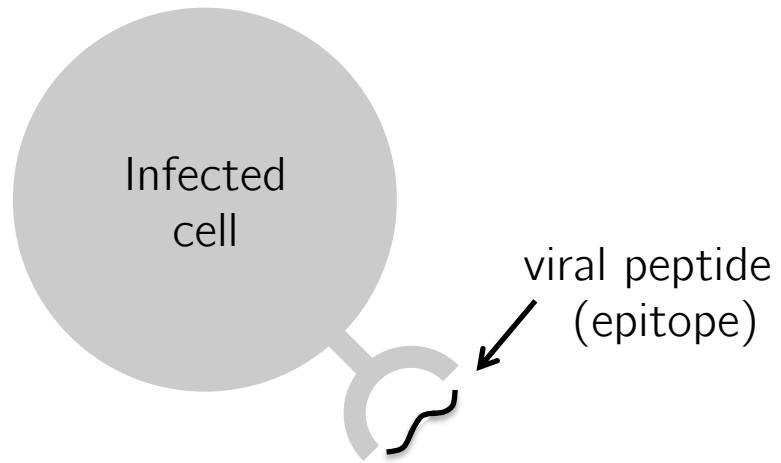


Statistical physics, inference, and the host-pathogen dynamics of HIV

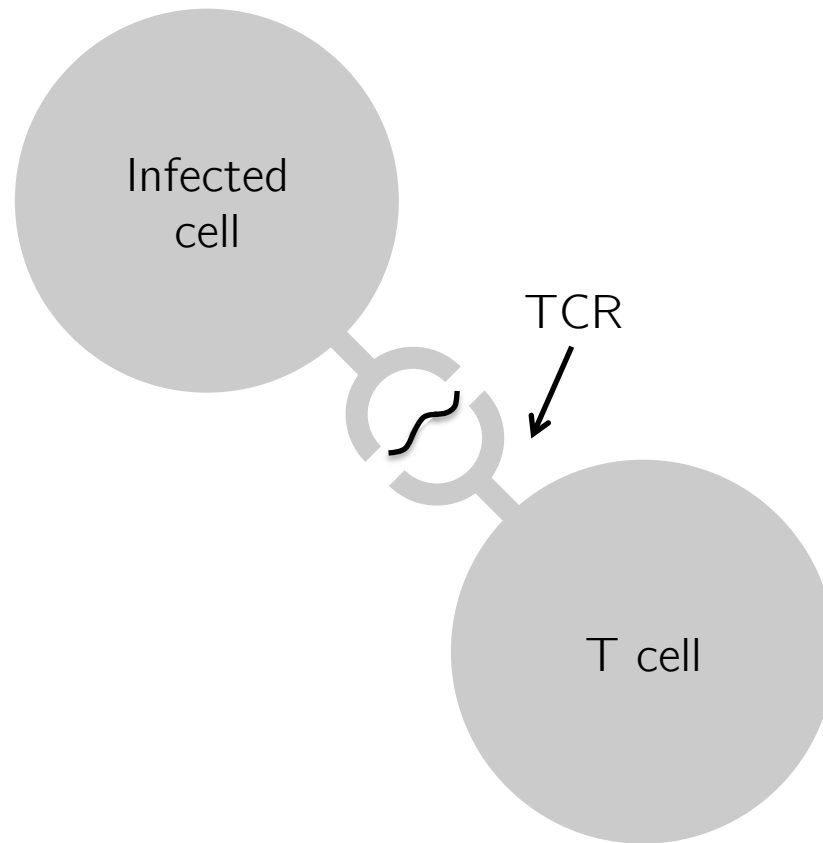
John Barton, MIT
Rutgers Statistical Mechanics Meeting
12-20-2016

Rapid evolution of HIV
prevents effective immune control of infection



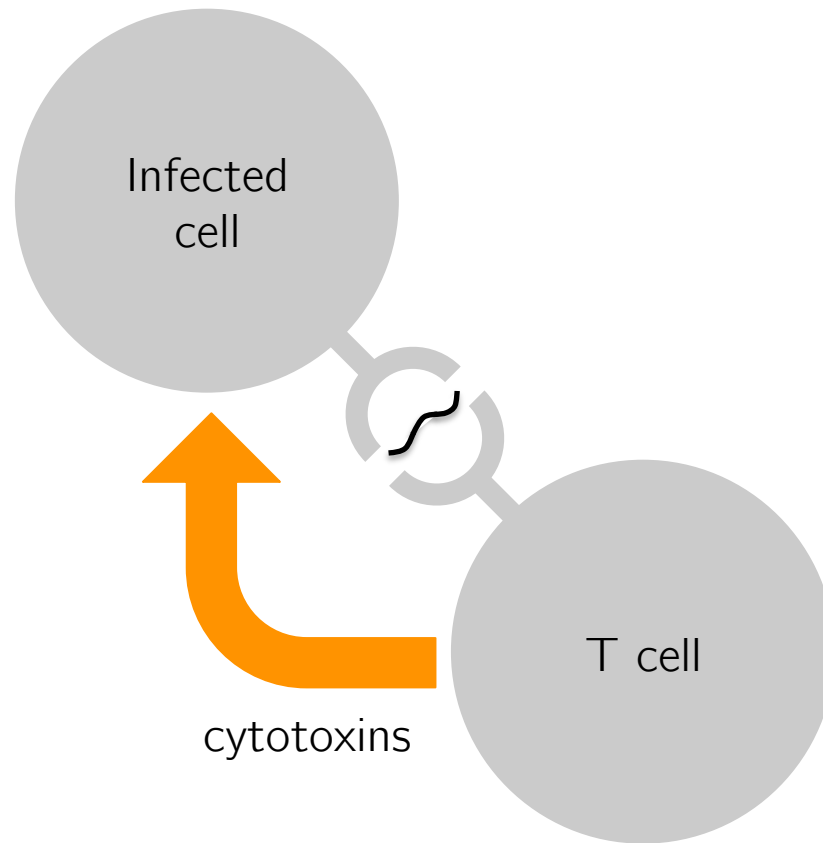
T cells kill infected cells
and help control infection

Rapid evolution of HIV
prevents effective immune control of infection



T cells kill infected cells
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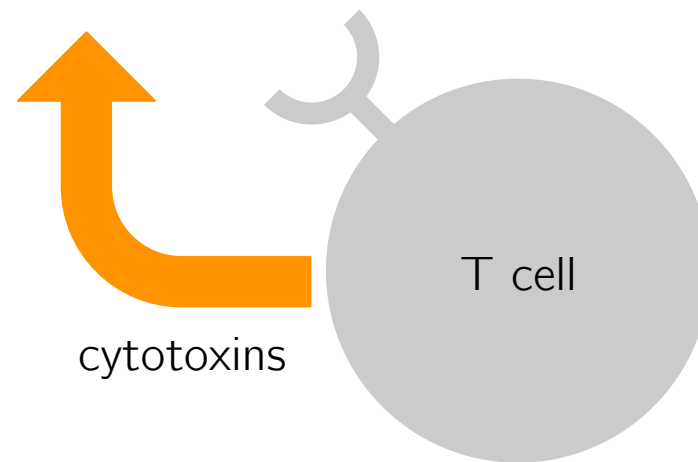
Rapid evolution of HIV
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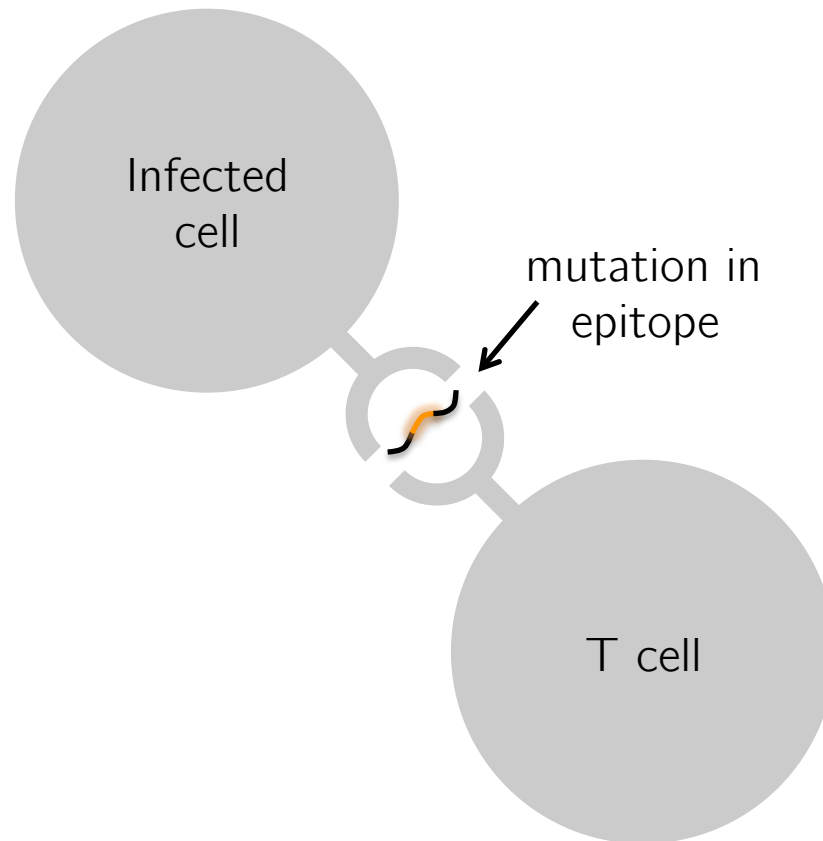
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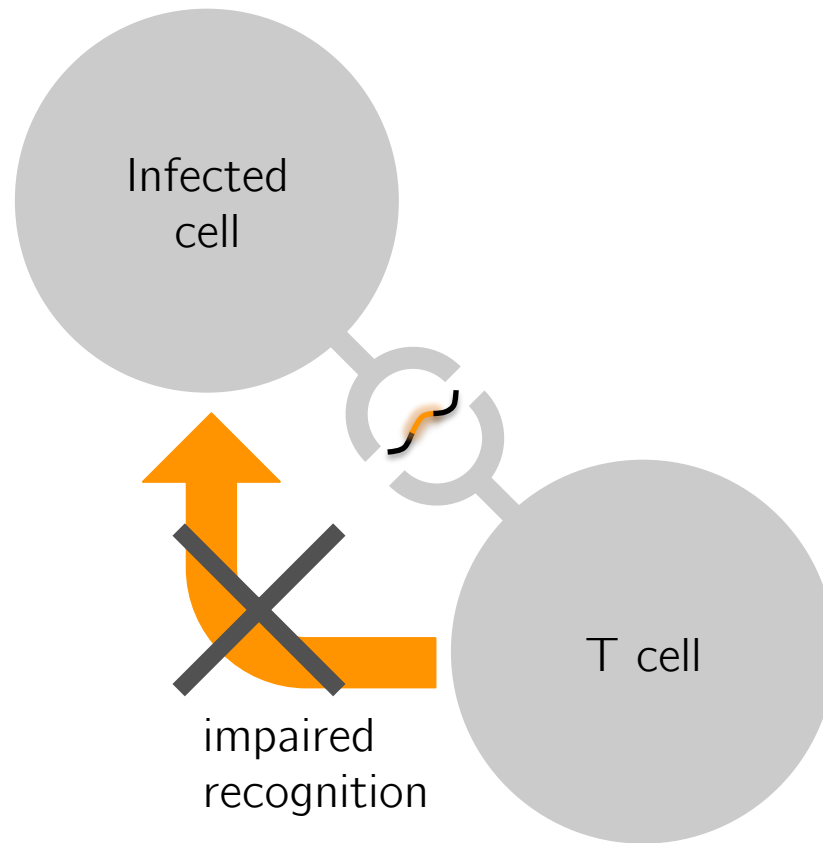
Rapid evolution of HIV
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T cells kill infected cells
and help control infection

Escape mutations
prevent T cell recognition
allowing replication to
continue unchecked

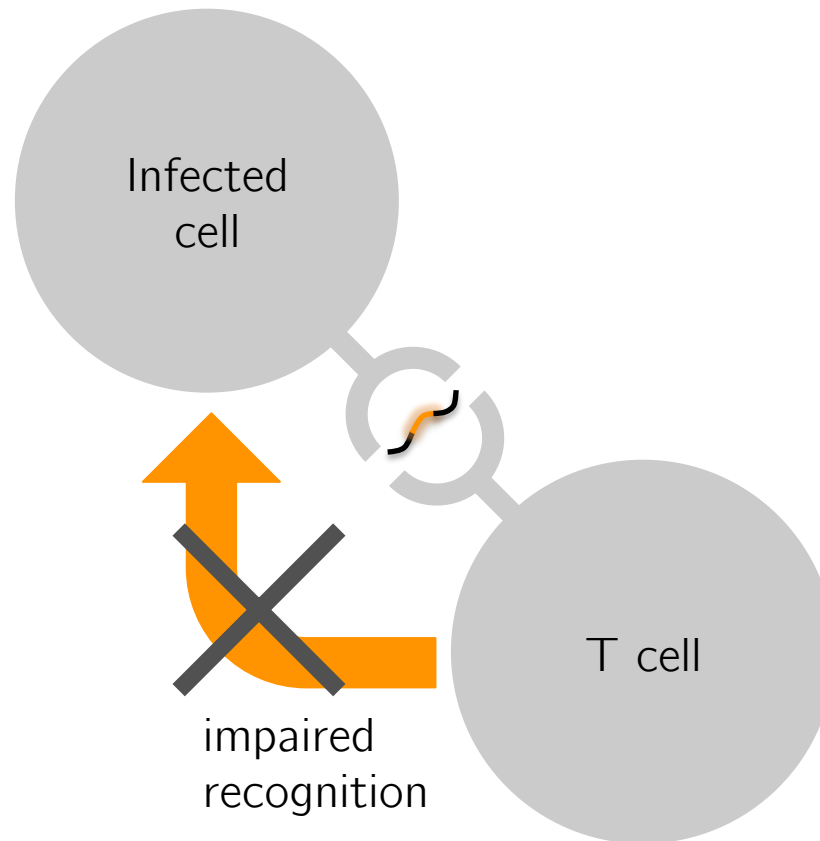
Rapid evolution of HIV prevents effective immune control of infection



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T cells kill infected cells
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Goal: identify **mutational
vulnerabilities** of HIV

Approach: use data to
identify parts of viral
sequences that are **highly
constrained**

Maximum entropy modeling

Statistical inference and model tests

Coevolution

Understanding how HIV escapes from
the immune system in vivo

Correlations quantify important constraints on HIV sequences

HIV sequences

M	G	A	R	A	S	V	L	S	G	G	E
M	G	A	R	A	V	V	L	S	G	G	K
M	G	A	R	A	V	V	L	S	G	G	K
M	G	A	R	A	S	V	L	S	G	G	E
M	G	A	R	A	S	V	L	S	G	G	K
M	G	A	R	A	S	V	L	S	G	G	Q



Consider a set of HIV sequences,
isolated from many different patients

We notice that

- some sites are more variable
- mutations are correlated

These properties are quantified by correlations,

frequency of observing amino acid α at site i : $p_i(\alpha)$

frequency of observing amino acids α, β at sites i, j : $p_{ij}(\alpha, \beta)$

What is the simplest (maximum entropy) model
consistent with these constraints?

Maximum entropy models allow us to map from sequence to fitness, but inference is challenging

The maximum entropy model reproducing the correlations is a Potts model

$$P(\underline{s}) = \frac{\exp(-E(\underline{s}))}{Z}, \quad E(\underline{s}) = - \sum_{i=1}^N \boxed{h_i(s_i)} - \sum_{i=1}^{N-1} \sum_{j=i+1}^N \boxed{J_{ij}(s_i, s_j)}$$

Fields and **couplings** are Lagrange multipliers enforcing the constraints

$$\sum_{\underline{s}} \delta(s_i, \alpha) P(\underline{s}) = p_i(\alpha)$$

$$\sum_{\underline{s}} \delta(s_i, \alpha) \delta(s_j, \beta) P(\underline{s}) = p_{ij}(\alpha, \beta)$$

Maximum entropy models allow us to map from sequence to fitness, but inference is challenging

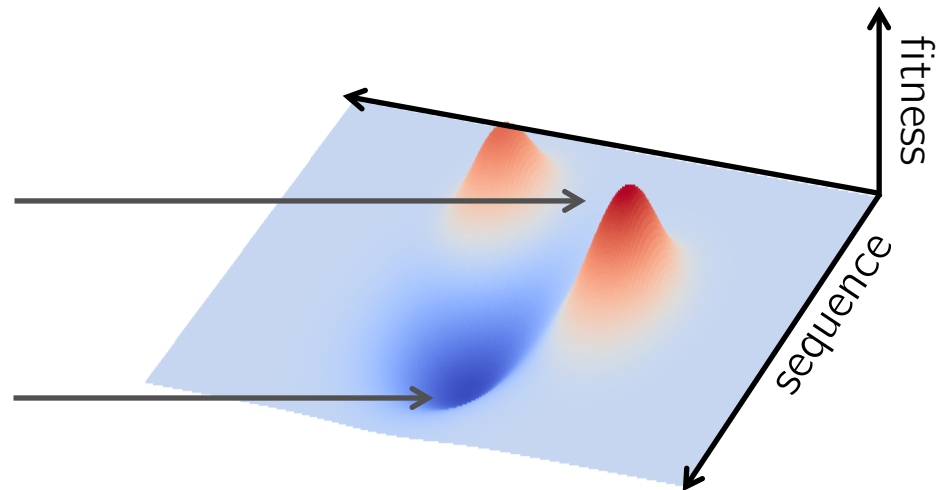
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Energy is negatively correlated with **fitness**

Most prevalent (low energy) sequences should be fittest

Rarely observed (high energy) sequences should be unfit



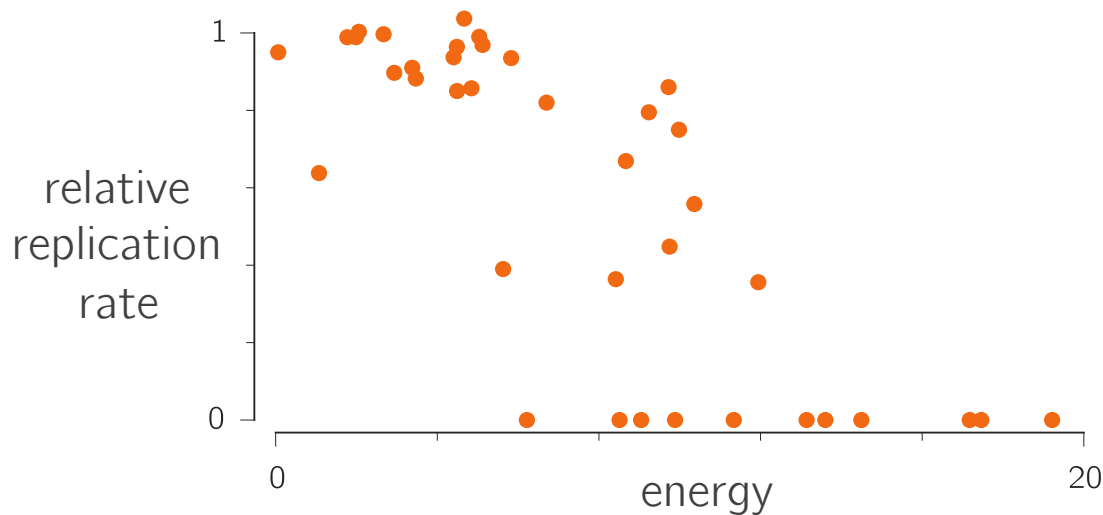
Ferguson et al, Immunity (2013)
Mann⁺, JPB⁺, Ferguson⁺ et al, PLOS Comp Biol (2014)

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Energy is negatively correlated with **fitness**

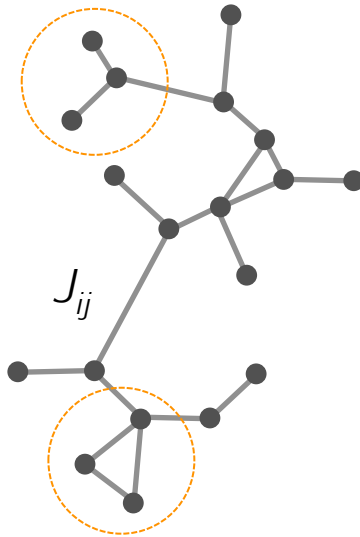
Need to find parameters that maximize the (average log-) likelihood

$$-\mathcal{L} = \log Z - \sum_i \sum_{\alpha} h_i(\alpha) p_i(\alpha) - \sum_{i,j} \sum_{\alpha,\beta} J_{ij}(\alpha, \beta) p_{ij}(\alpha, \beta)$$

$$Z = \sum_{\underline{s}} \exp(-E(\underline{s}))$$

Number of terms in Z is **exponential** in the system size

Adaptive cluster expansion (ACE) builds global solutions from local ones



Assumption: to accurately estimate the parameters, we can use local information

Formally, assume that the inverse susceptibility $\chi^{-1} = dJ/dp$ is short-ranged

Expand the likelihood (entropy) in terms of contributions from **clusters** of sites Γ

$$\mathcal{L} = \sum_{\Gamma} \Delta \mathcal{L}_{\Gamma}, \quad \boxed{\Delta \mathcal{L}_{\Gamma}} = \boxed{\mathcal{L}_{\Gamma}} - \sum_{\Gamma' \subset \Gamma} \Delta \mathcal{L}_{\Gamma'}$$

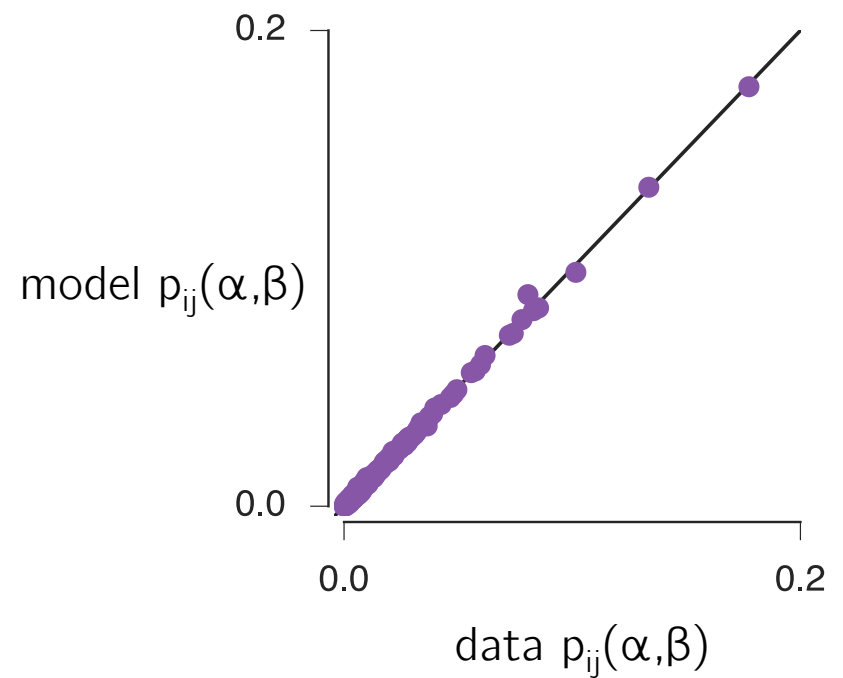
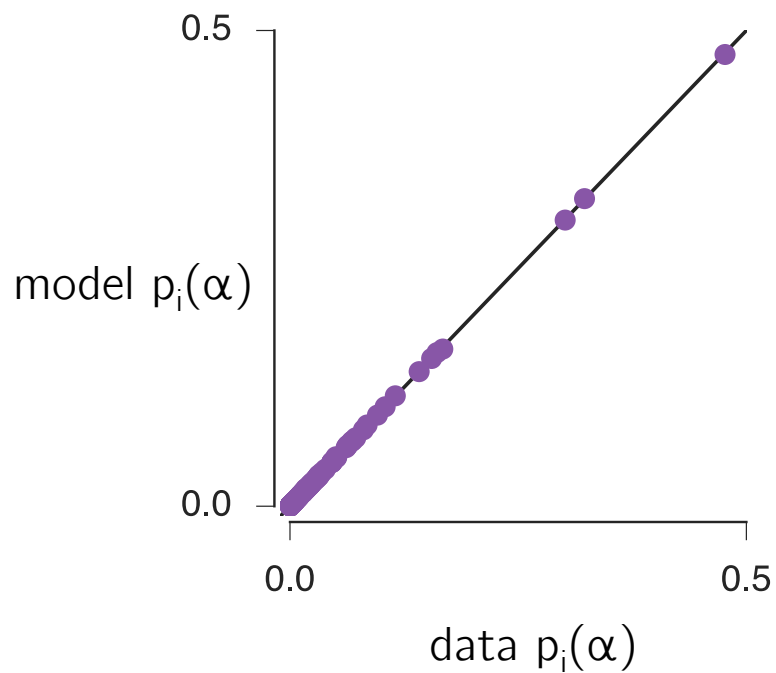
Likelihood of the model restricted to the sites in Γ alone

Contribution to the likelihood from the cluster Γ which is not captured by any subsets of Γ

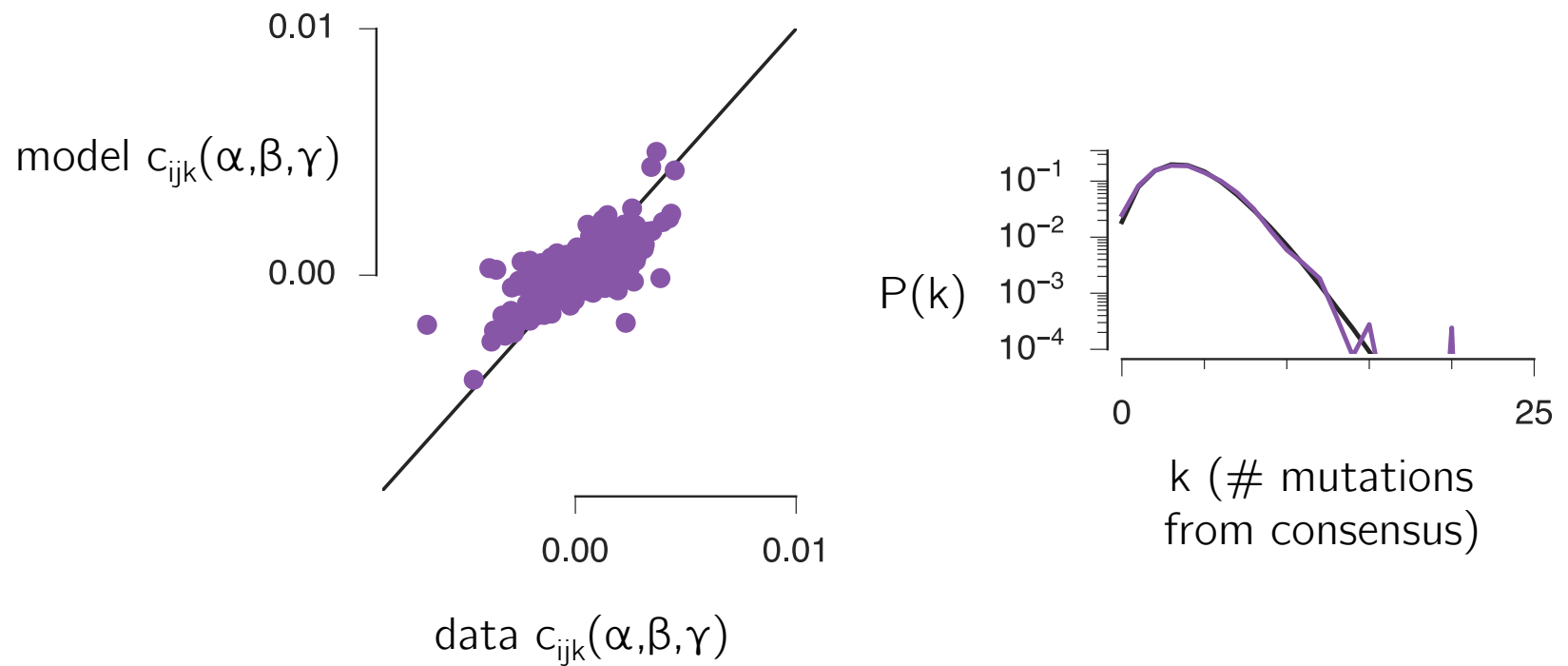
This **cluster expansion** may rapidly converge, can computationally select out largest terms (**adaptive**)

Cocco & Monasson, PRL (2011)
Cocco & Monasson, JSP (2012)
JPB & Cocco, JSM (2013)

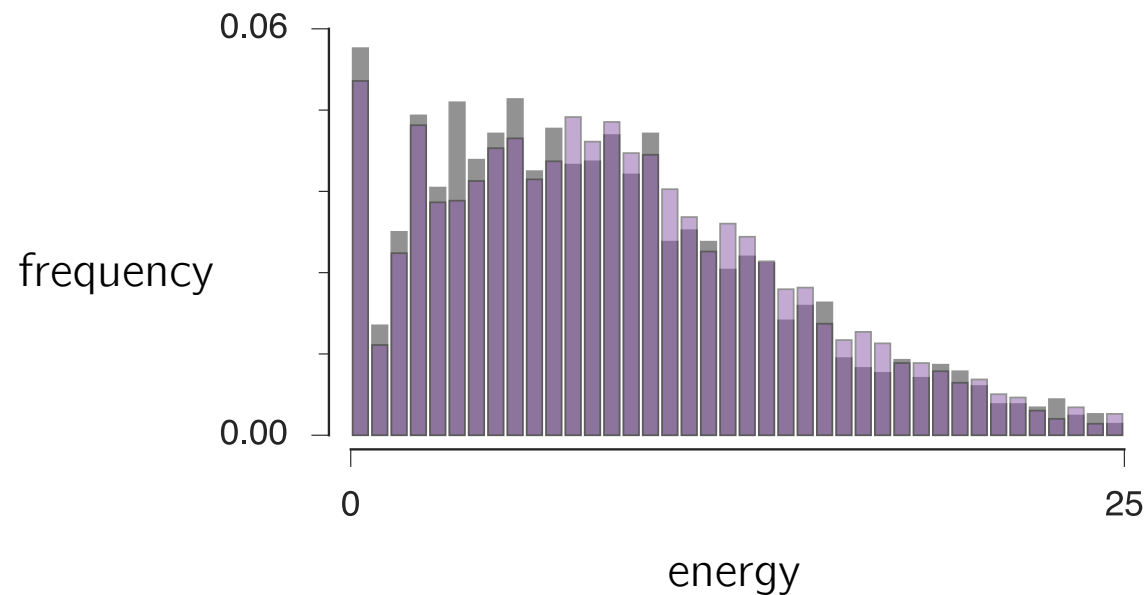
ACE accurately recovers statistics of the data,
including some higher order correlations



ACE accurately recovers statistics of the data,
including some higher order correlations



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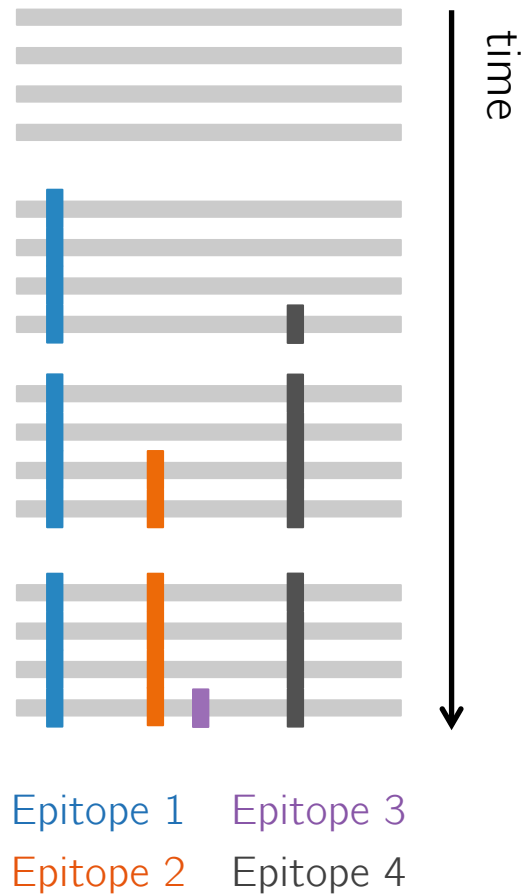
Distribution of energies
in the **model** matches
with the **data**, samples
are consistent

Maximum entropy modeling
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Understanding how HIV escapes from
the immune system in vivo

In vivo evolution of viral populations can be studied in clinical data



CHAVI longitudinal study of 17 individuals, starting from initial infection with follow-up over 1-3 years

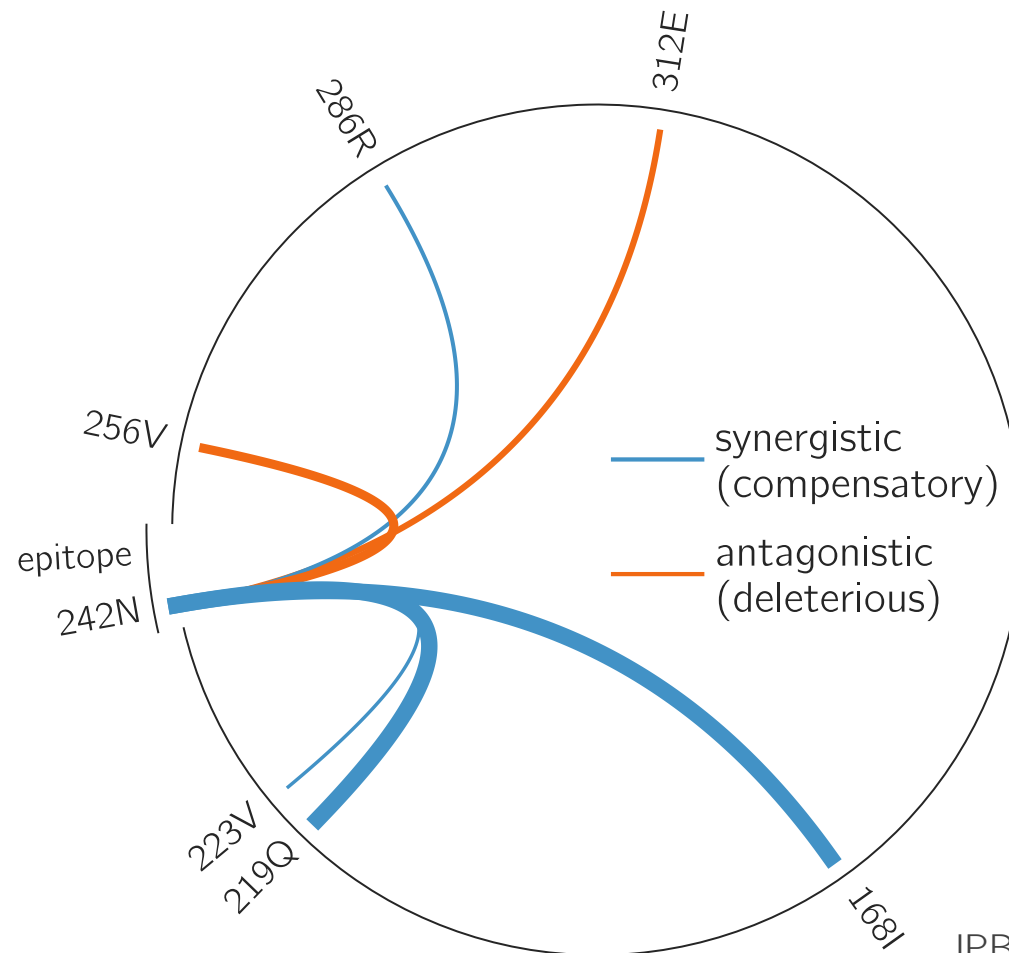
At each visit, sample sequences from the viral population, map T cell responses

We want to predict **timing** and **location** of escape mutations

Escape should be slower when mutation significantly increases E

The model captures effects of the viral sequence background on escape

Gag TW10 epitope is usually **protective** (high fitness cost of escape), but escaped rapidly in one patient



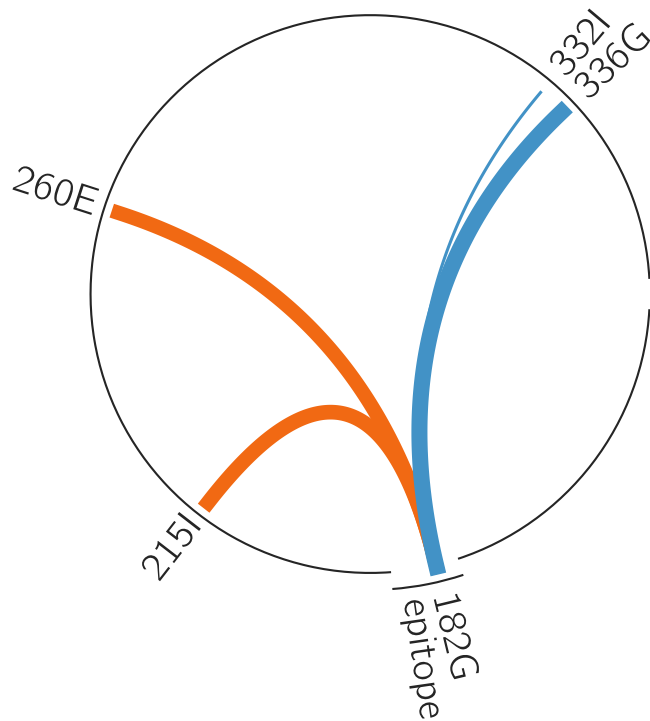
Plot of all strong ($|J| > 0.1$) interactions between escape mutation and the sequence background

Known compensatory mutations 219Q, 223V, reduce fitness cost of escape

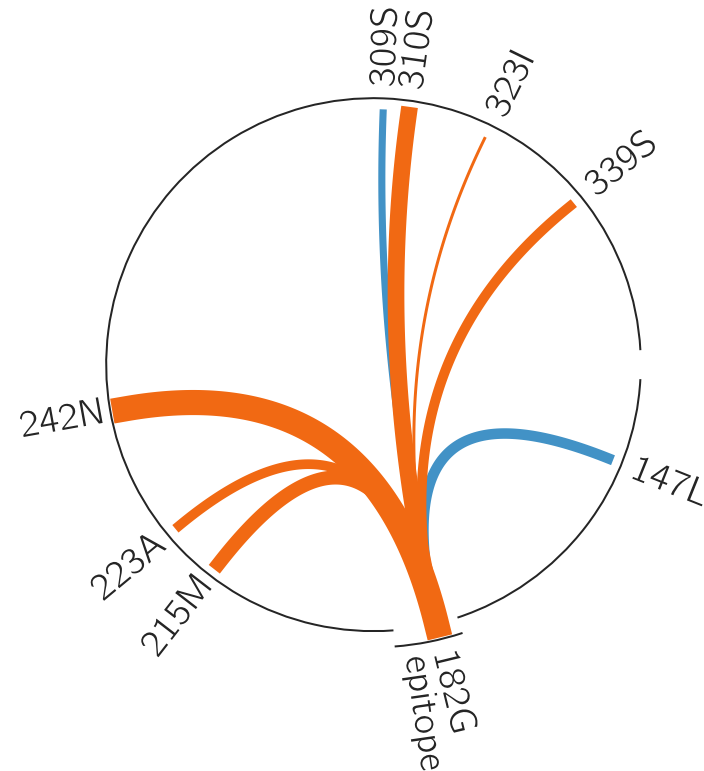
JPB et al., Nature Communications (2016)

The model captures effects of
the viral sequence background on escape

Identical epitopes targeted by different patients:



Escape after 120 days

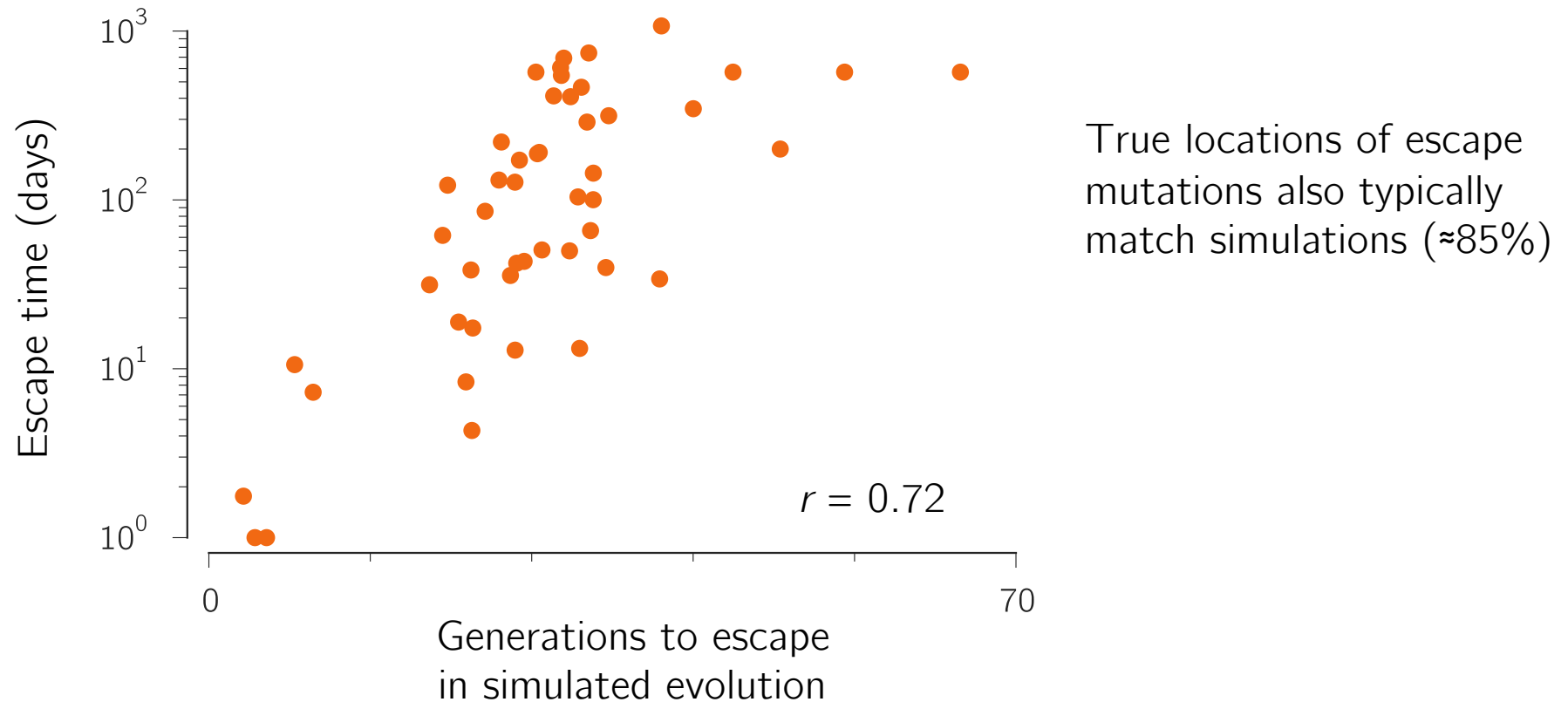


Escape never observed
(>1103 days)

JPB et al., Nature Communications (2016)

Simulate viral evolution by coupling the fitness landscape to a Wright-Fisher-like model

Simulate evolution of virus population, with selective advantage of escape **based on strength of immune response**
Measure number of generations to escape in simulation



Acknowledgments

MIT

Arup Chakraborty
Mehran Kardar
Thomas Butler
Kevin Kaczorowski
Dariusz Murakowski
Karthik Shekhar

UKZN

Thumbi Ndung'u
Jaclyn Mann
Erasha Rajkoomar

Ragon
Institute

Bruce Walker

Oxford

Andrew McMichael

UNC

Nilu Goonetilleke

UIUC

Andrew Ferguson

ENS

Rémi Monasson
Simona Cocco
Eleonora De Leonardi
Alice Coucke



Summary

- ACE infers excellent generative models from input HIV sequence data (and others, see github.com/johnbarton/ACE)
- HIV sequence data reveals information about the fitness landscape of the virus
- Given information about fitness, sequences in the viral population, and the immune response, escape from T cell pressure is predictable (probabilistically)
- Signals of host-pathogen coevolution imprinted in viral sequences JPB, Kardar, & Chakraborty, PNAS (2015)
- HIV protease drug resistance Butler⁺, JPB⁺, Kardar, & Chakraborty, Phys Rev E (2016)